



Design an Interval Type -2 Fuzzy PI & PID Controller for Nonlinear System

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ABSTRACT: An interval type-2 fuzzy logic controller (T2FLC) for nonlinear dead time process is proposed in this paper. Then PI & PID of T2FLC are applied to dynamic nonlinear system to analysis and comparative study of different performance parameter. Hence to comparative study of T2FLC with conventional T1FLC of different performance parameter such as rise time(t_r), peak overshoot(% m_p), settling time(t_s) integral absolute error (IAE) and integral-of-time multiplied absolute error(ITAE) are taken . In this work an improved performance of T2FLC is observed. A type-2 fuzzy controller is designed by blurred the membership function based on foot print of uncertainties (FOU) and embedded four T1FLC.

KEYWORDS: interval type-2 fuzzy controller, IAE, ITAE, blurred the membership function, FOU, embedded four T1FLC

I.INTRODUCTION

Conventional PID controller and fuzzy logic system (FLS) constructed based on type-1 fuzzy logic controller (T1FLC) referred to as T1FLS have shown their ability in many applications, especially for the control of complex nonlinear systems that are difficult to model analytically but they cannot be successfully handled the uncertainties[1] .We propose a type-2 fuzzy logic controller (T2FLC) to produce better system performance and to handle the uncertainties more in compared to PID and type-1 FLC. We design an embedded four type-1 FLC to produce type-2 FLC in this paper. With advantages offered by type-2 fuzzy systems (T2FS) in handling uncertainties to control different parameter in nonlinear process applications, one major problem that adverse effects its wide-spread implementation in real-time applications is its high computational cost (Hameed, 2010). In order to reduce the above effects of T2FS, a simplified T2FS based on a hybrid structure [2] of four type-1 fuzzy systems (T1FS) and a fuzzy based linguistic approach is applied in this paper. To check the robustness and reliability of the new implementation type-2 FLC, then it is applied to control different parameter for a nonlinear system equipped with various types of uncertainties. Because of T1FS are certain in the sense that for each input there is a crisp membership grade, but T2FS characterized by membership grades that are themselves fuzzy [3].

There are some recent works related to type-2 FLC for different process to encounter different uncertainties. Qilian Liang and Jerry M. Mendel described upper and lower membership function for the case of Gaussian primary MFs of type-2 FLC and show the better performance than type-1FLC (2000).Christopher Lynch, Hani Hagraas described the current speed controllers for marine/traction propulsion systems are based on type-2 Fuzzy Logic Controllers (T2FLC) shows that better performance with uncertainties than conventional PID and type-1 FLC (2005).Philip A compared the differences between type-1 (T1FLC) and interval type-2 fuzzy logic controllers (T2FLC) with seven, five and two three term membership functions. The controllers were used to control a DC motor model in a closed loop simulation (2009).Mohammad Biglarbegan, William W. Melek, Jerry M. proposed a novel inference mechanism for an interval type-2 Takagi–Sugeno–Kang fuzzy logic control system (IT2 TSK FLCS) when antecedents are type-2 fuzzy sets and consequents are crisp numbers (A2-C0) and applied it to teal time plant. Using LQR techniques they found stability with good satisfaction (2010).Erdal Kayacan, Okyay Kaynak, Rahib Abiyev, Jim Tørresen, Mats Høvin and Kyrre GletteAbstract—Type-2 fuzzy logic systems are proposed as an alternative solution in the literature when a system has a large amount of uncertainties and type-1 fuzzy systems come to the limits of their performances. In this study, an adaptive type-2 fuzzy-neuro system is designed for the position control of a servo system with an intelligent sensor. (2010).Ondrej Linda presented a comparative analysis of interval T2 (IT2) and T1 FLCs in the context of learning



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behaviors for mobile robotics. Where a T1 FLC is optimized using the Particle Swarm Optimization algorithm to mimic a wall-following behavior performed by an operator. Next, an IT2 FLC is constructed by symmetrically blurring the fuzzy sets of the original T1 FLC (2011). Malik Manceur recently described a new second-order sliding-mode type-2 fuzzy controller for nonlinear uncertain perturbed systems. The control is based on the super-twisting algorithm, which is among second-order sliding-mode controls (SMCs) (2012). Michal Blaho, Martin Urban, Peter Fodrek, Martin Foltin described the network disadvantages as uncertainty and reduced them with type-2 fuzzy logic controller (2012). Yang Chen, Tao Wang investigated the interval type-2 fuzzy PID control under Gaussian and triangular primary membership functions for different nonlinear systems (2012). Yazmin Maldonado¹ and Oscar Castillo¹ proposed the design of a Type - 2 Fuzzy Logic Controller (T2 - FLC) using Genetic Algorithms (GAs). The T2 - FLC was tested with different levels of uncertainty to regulate velocity in a Direct Current (DC) motor. (2013). Yang-Yin Lin, Jyh-Yeong Chang, Nikhil R. Pal, and Chin-Teng Lin, In this paper, a mutually recurrent interval type-2 neural fuzzy system (MRIT2NFS) is proposed for the identification of nonlinear and time-varying systems. The MRIT2NFS uses type-2 fuzzy sets in order to enhance noise tolerance of the system. In the MRIT2NFS, the antecedent part of each recurrent fuzzy rule is defined using interval type-2 fuzzy sets, and the consequent part is of the Takagi–Sugeno–Kang type with interval weights (2013). Ahmad M. El-Nagar *, Mohammad El-Bardini proposed an embedded real-time interval type-2 fuzzy proportional – integral – derivative (IT2F-PID) controller which is a parallel combination of the interval type-2 fuzzy proportional – integral (IT2F-PI) controller and the interval type-2 fuzzy proportional – derivative (IT2F-PD) controller with uncertainties. The proposed IT2F-PID controller is implemented practically using a low cost PIC microcontroller for controlling the uncertain nonlinear inverted pendulum to minimize the effect of the system uncertainties and found significant improvement result (2014). This paper is organized in this way as follows. Section II describes type-1 FLC method. Section III presents type-2 FLC for nonlinear process. Section IV gives the case studies with the proposed T2 FLC PID/PI controller. The simulation results are compared between T1 FLC and T2 FLC. Finally last section presents conclusion and future scope of the works.

II. TYPE-1 FLC

The design of fuzzy controller are based on different step. In the first step fuzzy controller is to determine the inputs and the output of the fuzzy system where the error between reference and actual model output is $e(t)$ and its time derivative are taken as the system input and the controller output is considered as fuzzy system output [6]. The linguistic variable which are tabulated in table-1 in below are considered as the size of the input and the output. The shape of the membership function of these rules are a very important factor in the design of a controller. The shapes are trapezoidal, bell curve function, triangular function, out of these shapes last one is taken as the shape of the membership function in this paper because of its simple computation method. The other important factor must be considered for the designs of membership function are the number of curve and their position. The input and output are normalized to vary between -1 to +1 using the scaling factor of the gain in the simulation block. The linguistic variable 'PS', 'NS' and 'NB', 'PB' are strongly influence the steady state error of the system and the initial undershoot, overshoot, respectively following disturbances. The magnitude of controller input is strongly influenced by both error and the deviation error. The values which are commanding the fuzzy system response are shown in table. We select Mamdani method to implement the inference engine to improve the performance of PID & PI controller using min function method [13]. Bisection method is used for the defuzzification to convert the fuzzy output to the crisp output. To improve the robustness of the controller against parameter uncertainties and external disturbances, the controller must be based on fuzzy logic. Where the error input dominates the output of the fuzzy control indicating that the fuzzy side of the controller has to compensate particularly the proportional gain under deficiency condition.

III. TYPE-2 FLC

FLS constructed on the basis of type-1 fuzzy system referred to as T1FLS have shown its ability in many linear and especially for the control of complex non linear system which are more difficult to model analytically [1]. So the model difficulty and uncertainty effect cannot able to reduce by T1FLS due to crisp membership grade for each step of variation. Now the above effect is reduced by T2FLS because it characteristics by membership grades that are themselves fuzzy. The MF of T2FLS represents the uncertainties in the shape and position of the T1FLS [2]. The uncertainties is bounded up by upper MF and LF both of which are of T1FLS. So the uncertainties of T2FLS are very useful in a situation where it is difficult to measure exact membership grade for FS. Because of better capabilities to



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handle linguistic uncertainties by modelling and unreliability of information, the amount of uncertainties in a system could be reduced by T2FLS and now it is in a condition to outperform its T1 counterpart.

As it is known that the MF of a T2FS has a footprint of uncertainty (FOU), which represents the uncertainties in the shape and position of T1FS [16]. The FOU is bounded up by an upper MF (UMF) and by a lower MF (LMF), both of which are T1MF. Since the FOU of T2FS provides an extra mathematical dimension, they are very useful in circumstances where it is difficult to determine an exact membership grade for FS. Therefore, the amount of uncertainty in a system could be reduced by using T2FLS since it offers better capabilities to handle Fuzzy Controllers. Triangular type membership function of type -2 FS is done by (a) blurring the width of type-1 FS (b) blurring the centre of type-1 FS. Ability of T2FLS is to reduce the unwanted oscillation by the control surface of a T2FLS which is smothering than that of T1FLS especially around the origin which is added that of T1 counterpart. Due to small disturbances around steady state, the output of T2FLS will not produce significant control signal. As a result; this will minimize the amount of oscillation. So additional degree of freedom provided by the uncertainties of T2FLS is used to handle modelling uncertainties compared to conventional T1FLS. The performance of a designed controller of a model will naturally deteriorate after application to an actual plant due to unable to consider all the characteristics of the plant. Now if a controller T2FLS is designed to handle modelling uncertainties would be effective [13].

Hence in this work, T2FLS could be obtained by blurring a T1FLS. Now the membership function with uncertainties width is created by blurring its width and keeping its centre fixed compared to conventional T1FLS. So in this paper, for the sake of simplicity MF with uncertainties width has been adopted. The performance of a designed controller of a model will naturally deteriorate after application to a actual plant due to unable to consider all the characteristics of the plant. Now if a controller T2FLS is designed to handle modelling uncertainties would be effective.

A set of an infinite number of T1FS is the basic structure of T2FLS and the defuzzified output of T2FLS could be calculated by aggregating the centroid of the infinite number of embedded T1FLS. When the antecedent membership grade [16] in T2FLS have a continuous domain, the number of embedded T1FLS becomes uncountable. In this paper, for each T2FLS will be represented by its upper and lower bounds which are T1 membership function. Therefore, each two neighbour T2MFS will intersect in four points in compared with T1MFS with one point intersections. The four intersection points are named as upper points, right points, lower points, left points which are shown in the following block diagram[8]. Membership function for the upper intersection points are constituted by the combination of the right side of the upper band of each T2MF with the left side of the upper bound of its neighbour. Similarly membership function for the lower intersection points are constituted by right side of the lower bounds of each T2MF with left side of the upper bound of each neighbour. In this way membership function of the four intersection points are constructed with each intersection point occurs equally likely to each of the intersection points. So the membership function for upper, right, lower, left intersection points will be used as input and output MF of the upper, right, lower, left fuzzy block respectively. The defuzzified output of T2FLS is then obtained by averaging defuzzified output of the resultant effect of the four embedded T1FLS. When the uncertainties value equals zero, then four intersection points becomes one and as a result T2MF will behave like T1MF. According to the level of uncertainties detected in this system, T2FLS and T1FLS will vary in between them. Interval type -2 fuzzy systems consist of four stages; they are fuzzification, inference, type reduction, and defuzzification. The fuzzification maps a numeric value $x=(x_1, \dots, x_p)^T \in x_1, x_2, x_3, \dots, x_p = x$ on a type- 2 fuzzy set A_x in X where A_x is a singleton fuzzy set and if $\mu_{A_x} = 1/1$ at $x=x'$ and μ_{A_x} at $x \neq x'$ [17]. The inference stage consist of two block, they are the rules and the inference engine. Working principle of the inference block is the same way for type -1 fuzzy system except the antecedent fuzzy sets the consequent are represented by type -2 fuzzy sets. The combination of rules and mapping the input to the output is done by join and meet operation. A type reducer is used to convert from type-2 to type -1 fuzzy interval on the output. Defuzzification step consist of obtaining a numeric value for the output which is an average value.



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Table 1: 49 rules and 25 rules for seven term and five term type1 FLC and type-2FLC respectively

$\Delta e/e$	NB	NM	NS	ZE	PS	PM	PB
NB	NB	NB	NB	NB	NM	NS	ZE
NS	NB	NM	NM	NM	NS	ZE	PS
NM	NB	NM	NS	NS	ZE	PS	PM
ZE	NB	NM	NS	ZE	PS	PM	PB
PS	NM	NS	ZE	PS	PS	PM	PB
PM	NS	ZE	PS	PM	PM	PM	PB
PB	ZE	PS	PS	PB	PB	PB	PB

$\Delta e/e$	NB	NM	ZE	PM	PB
NB	NB	NB	NB	MN	ZE
NM	NB	NB	NM	ZE	PM
ZE	NB	NM	ZE	PM	PB
PM	NM	ZE	PM	PB	PB
PB	ZE	PM	PB	PB	PM

IV. RESULT

In this section we considered nonlinear processes with dead time to show the simulation results for T1FLC & T2FLC. To get clear comparison between T1FLC & T2FLC, we measure several performance indices such as peak overshoot(%), rise time(t_r), settling time(t_s), IAE, ITAE are used. The values of the different performance indices are listed in the table 2. Peak overshoot and settling is considerably reduced with nearly same rise time for the T2FLC in compared with T1FLC. Hence IAE and ITAE are of two important factor because of they reflect the transient and steady state characteristics of a control system respectively.

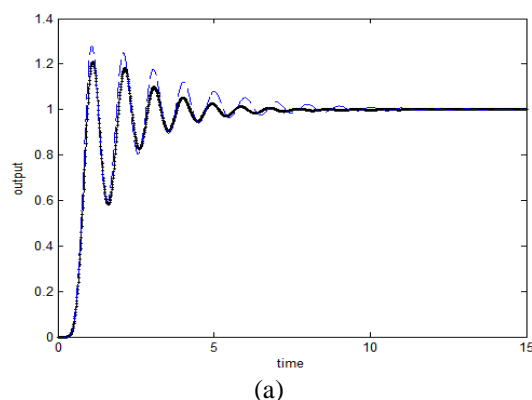
To setup the robustness of the proposed scheme for the above processes with different values of dead time we apply the same rule bases for both T1FLC and T2FLC and MF's with Mamdani method. For the numerical integration we use fourth-order Runge–Kutta method with an interval of 0.01 s for the simulation of the processes.

To performance analysis of PID type both for T1FLC and T2FLC

1) Second order nonlinear process: the process transfer function

$\ddot{y} + \dot{y} + 25y^2 = u(t-L)$, using this nonlinear process with different dead time $L=0.1, 0.3, \text{ and } 0.5$ with $G_e = 0.9, G_{\Delta e} = 11$ at $t=30s$ in each case for the design of T1FLC & T2FLC based PID controller and PI controller for the same but with different values of $G_e = 0.9, G_{\Delta e} = 13.5$. The different values of the performance indices are listed in table 2 and 3 and the response are shown in fig 4 and 5 with different dead time $L=0.3, 0.4 \text{ and } 0.5$ both for T1FLC (PID&PI) and T2FLC (PID &PI). It is clear from the comparison table that the T2FLC is shown better result than T1FLC both for PID and PI controller.

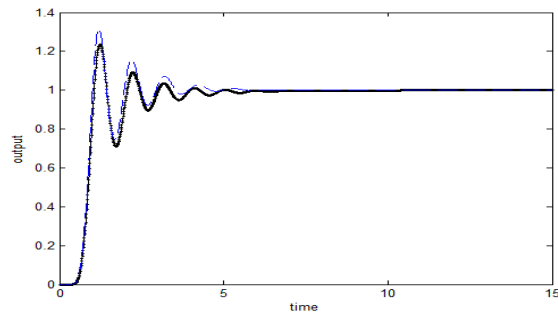
IV.1 PID Analysis



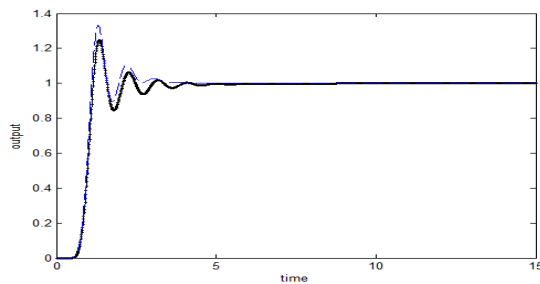
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(b)



(c)

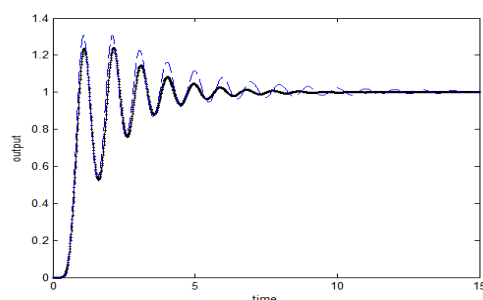
Fig 1 : $\ddot{y} + \dot{y} + 25y^2 = u(t-L)$ response with delay = 0.3, 0.4, 0.5 in (a), (b), (c) where solid line and dotted line represented for T2FLC (PID) & T1FLC (PID) respectively.

Performance analysis for the nonlinear system (PID)

Table 2: numerical value to compare T1FLC (PID) and T2FLC (PID) with different values of delay 0.3, 0.4, 0.5 respectively

Non linear equation	Delay(L)	Type of FLC	Rise time(t_r) sec	Settling time(t_s) sec	Peak overshoot (%)	IAE	ISE	ITAE	ITSE
$\ddot{y} + \dot{y} + 25y^2 = u(t-L)$	0.3	T2FLC	0.61	5.52	21.042	1.20	1.45	36.211	43.70
		T1FLC	0.56	8.08	28.06	1.34	1.80	40.29	43.70
	0.4	T2FLC	0.61	4.7	23.59	1.15	1.32	34.55	39.80
		T1FLC	0.56	4.3	31.42	1.12	1.27	33.80	39.80
	0.5	T2FLC	0.61	3.76	24.61	1.14	1.31	34.39	39.43
		T1FLC	0.56	3.25	33.21	1.11	1.23	33.39	39.43

IV.2 PI Analysis

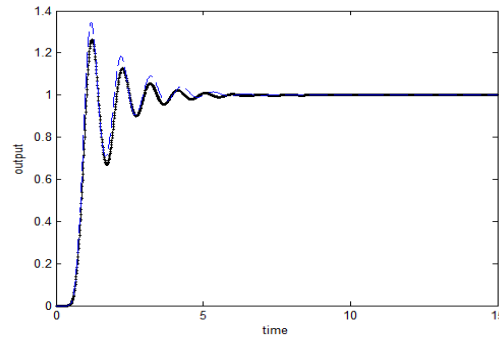


(a)

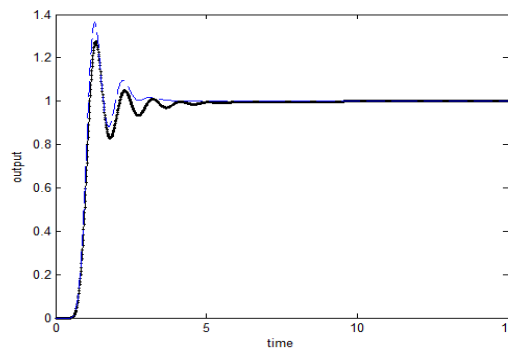
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(b)



(c)

Fig 2 : $\ddot{y} + \dot{y} + 25y^2 = u(t-L)$ response with delay = 0.3, 0.4, 0.5 in (a), (b), (c) where solid line and dotted line represented for T2FLC (PI) & T1FLC (PI) respectively.

Performance analysis for the nonlinear system (PI)

Table 2: numerical value to compare T1FLC(PI) and T2FLC(PI) with different values of delay

Non linear equation	Delay(L)	Type of FLC	Rise time(t_r) sec	Settling time(t_s) sec	Peak overshoot (%)	IAE	ISE	ITAE	ITSE
$\ddot{y} + \dot{y} + 25y^2 = u(t-L)$	0.3	T2FLC	0.60	6.38	23.99	1.32	1.74	39.62	52.33
		T1FLC	0.55	10.10	30.62	1.52	2.31	45.65	52.53
	0.4	T2FLC	0.59	4.65	26.45	1.16	1.36	35.07	41.00
		T1FLC	0.55	4.48	34.42	1.18	1.39	35.40	41.00
	0.5	T2FLC	0.59	3.38	27.63	1.16	1.35	34.91	40.63
		T1FLC	0.55	2.58	36.40	1.11	1.24	33.41	40.63

V. CONCLUSION

The proposed controller is designed based on interval type-2 fuzzy logic with footprint uncertainties which is more effective than type -1. Our proposed type-2 fuzzy PI & PID controller exhibited effective and showed better performance than type-1 fuzzy based controller.



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